



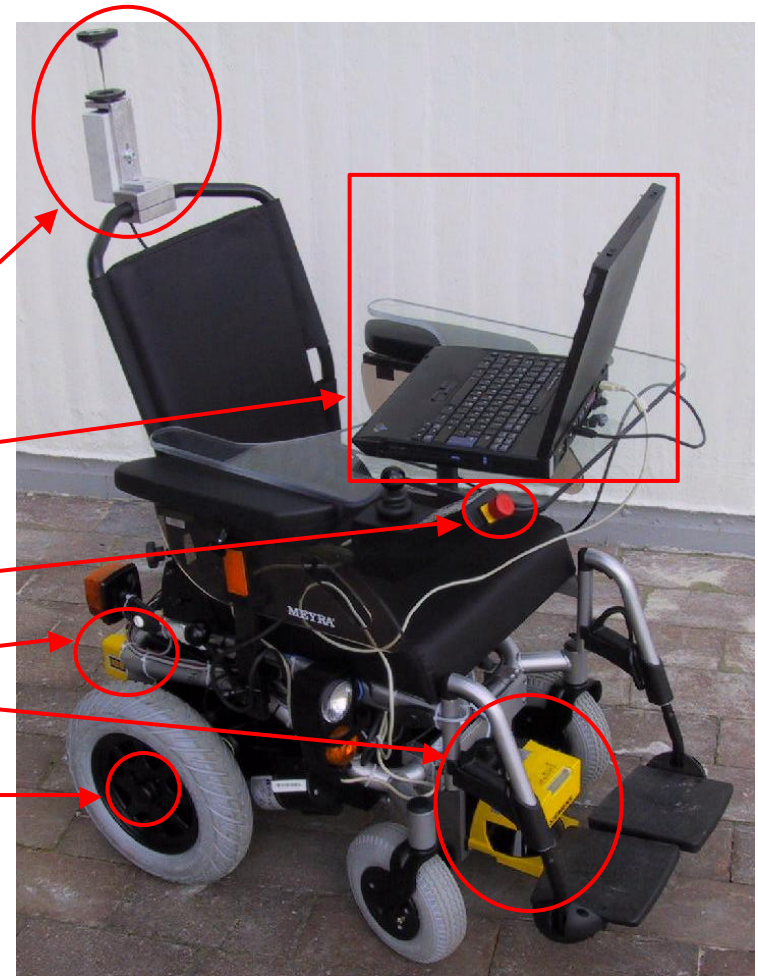
An Extension to the Dynamic Window Approach for arbitrarily shaped Robots

Overview

- Rolland: new hardware platform
- Motivation
- Basic principles of the **D**ynamic **W**indow **A**pproach
- DWA & the problem with non circular shaped robots
- Implementation issues: Curve Segments Table, Collision Table
- Computing the Trajectory
- Computing the Velocity Profile
- What remains to do
- Preliminary Experiments

- Rolland: hardware platform

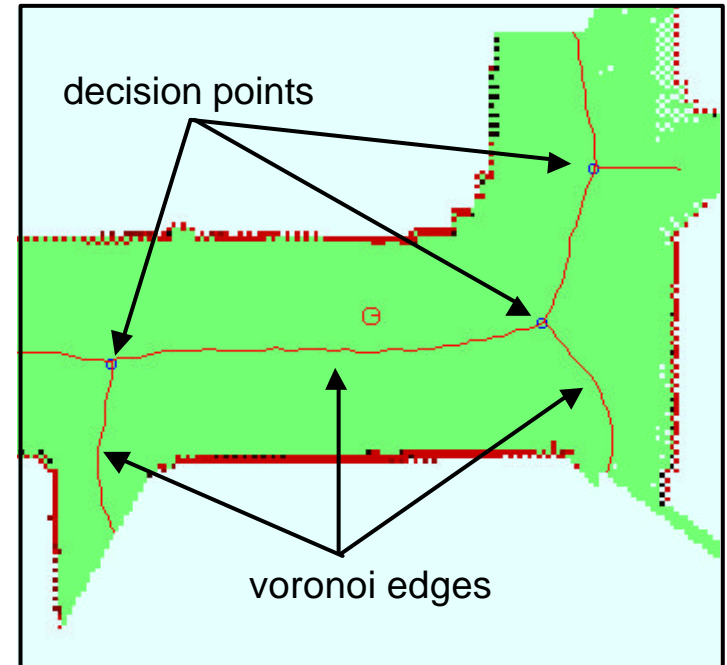
- Meyra Champ wheelchair
- omnidirectional camera system
- controlling laptop connected via single usb cable
- emergency stop button
- 2 laser range finder
- 2 incremental encoders



Motivation



Wheelchair in its environment

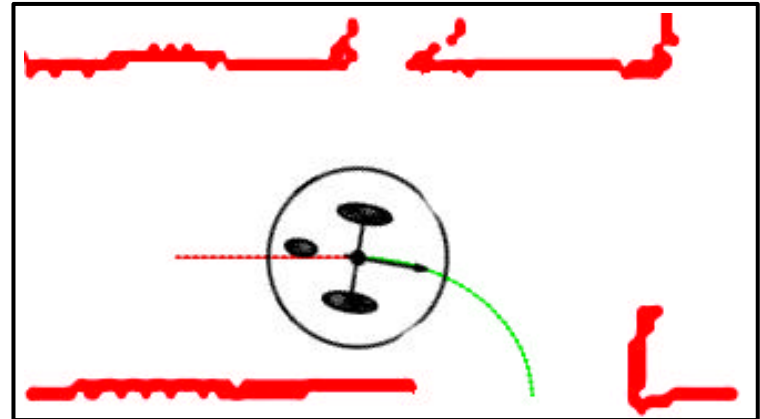


Metrical & topological representation.

How to navigate between decision points while taking care of dynamic obstacles?

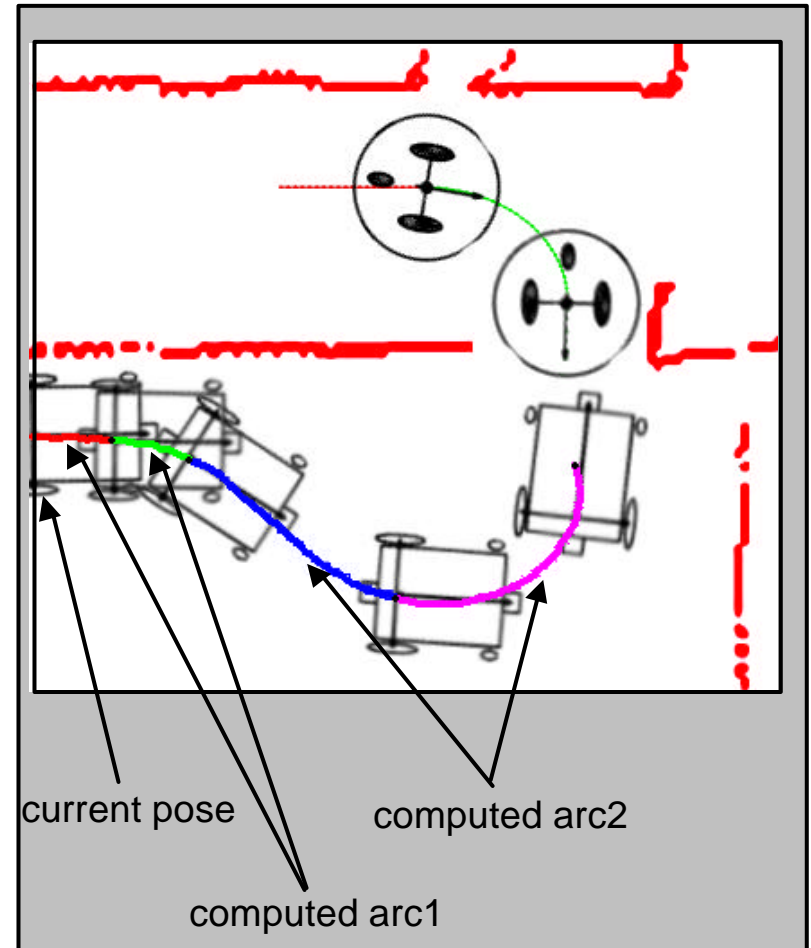
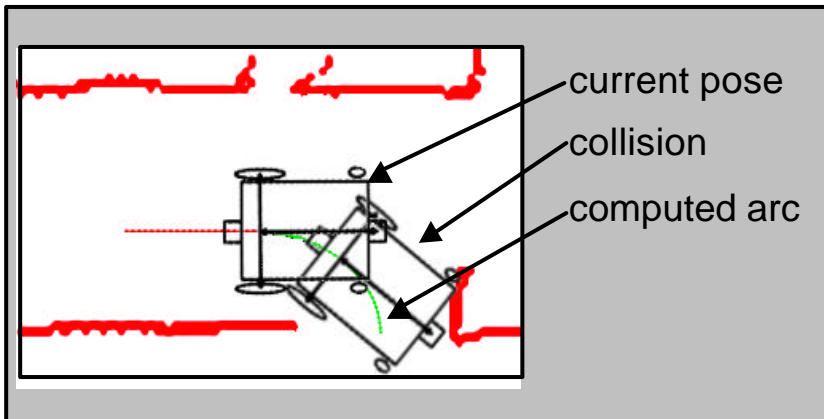
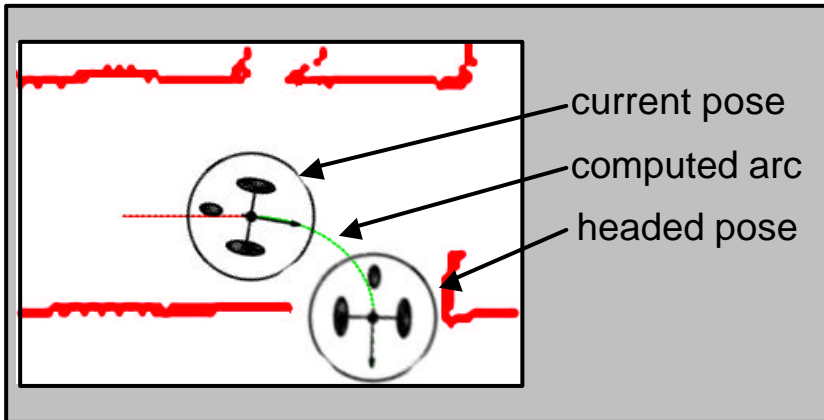
Basic principles of the **Dynamic Window Approach**¹

- Local navigation combined with reactive collision avoidance.
- **DWA** assumes: Robot velocity is a piecewise constant function in time.
- **DWA** considers: Robot has initial velocity and limited accelerations
- **DWA** computes optimal circular arc in every time step.
- **DWA** looks one curve ahead.

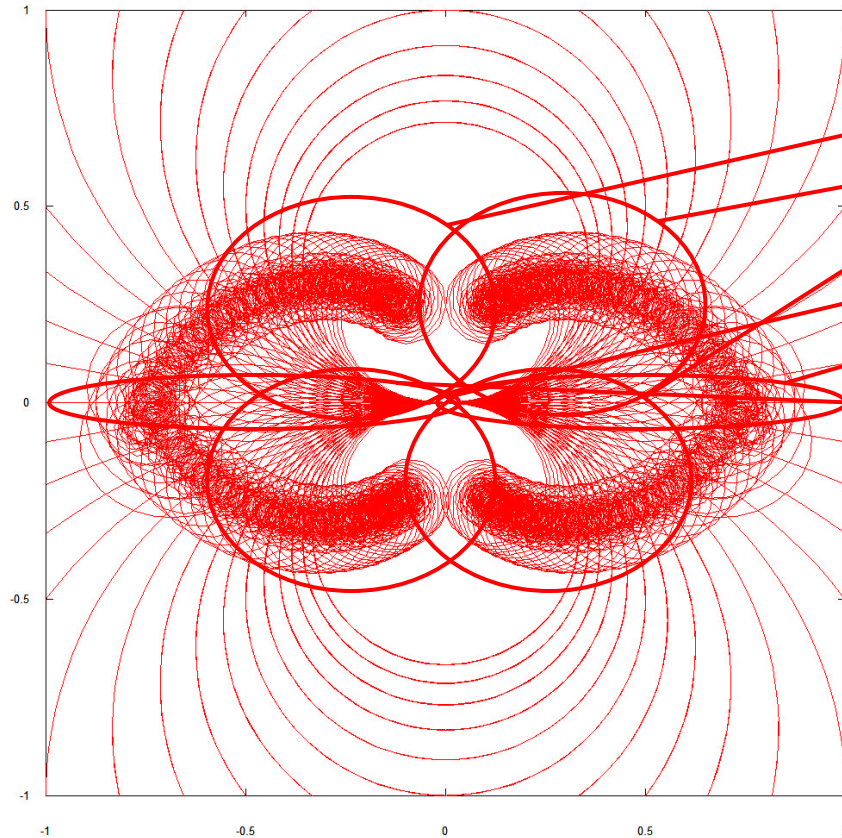


¹ [Fox, Burgard, Thrun] „The Dynamic Window Approach To Collision Avoidance“

DWA & the problem with non circular shaped robots



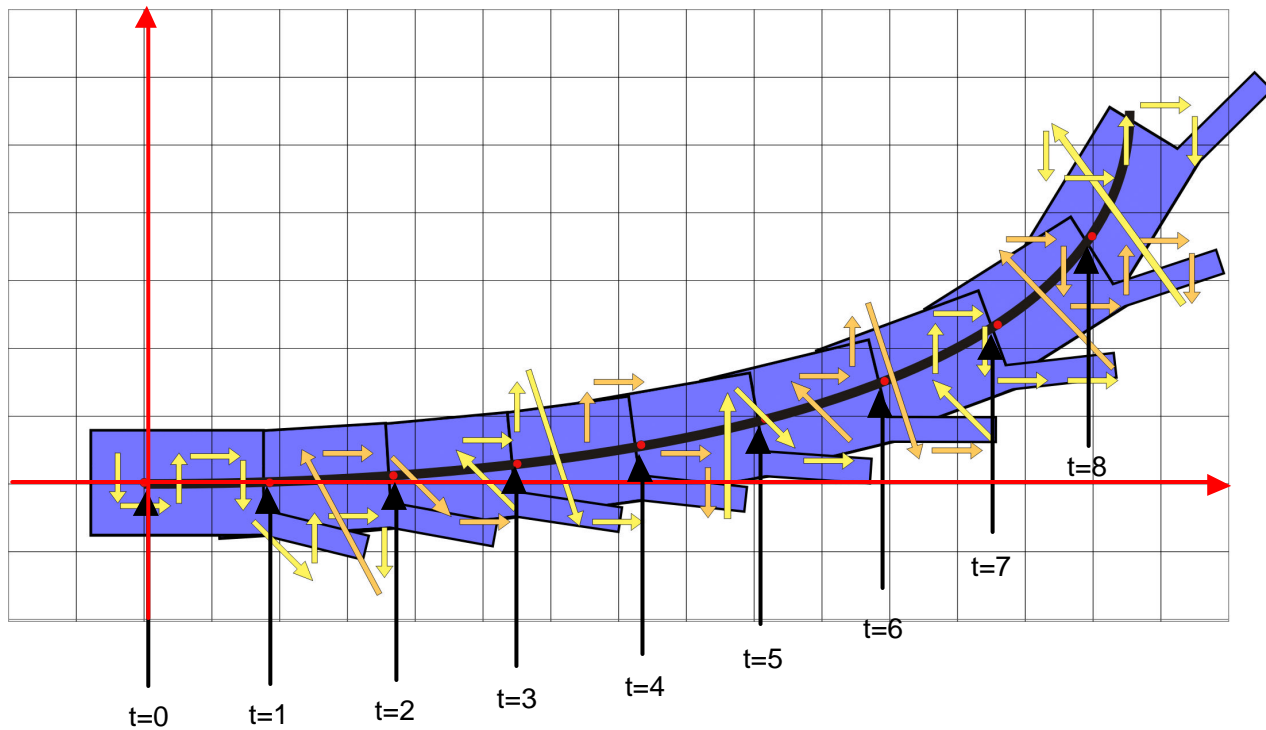
Curve Segments Table



start curvature	curvature prime	direction	poses
0	+ MAX	backwards	$(x_0, y_0, \mathbf{q}_0), \dots$
0	- MAX	forwards	$(x_0, y_0, \mathbf{q}_0), \dots$
0	+ MAX	forwards	$(x_0, y_0, \mathbf{q}_0), \dots$
0	- MAX	backwards	$(x_0, y_0, \mathbf{q}_0), \dots$
0	0	forwards	$(x_0, y_0, \mathbf{q}_0), \dots$
0	0	backwards	$(x_0, y_0, \mathbf{q}_0), \dots$
...

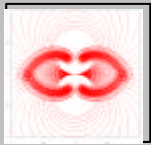
Collision Table

arclength (t)	0	...
offset between occupied cells ($\{(x_1, y_1), \dots, (x_n, y_n)\}$)	$\{(0, -1), (1, 0), (0, 1), (1, 0), (0, -1), (1, -1), (0, 1), (1, 0), (0, -1)\}$...

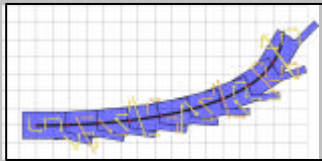


Algorithmic Refinements 1

Goal:
reduce Size of



Curve Segments Table



Collision Table



Precompute and store only paths whose first pose
has zero heading.

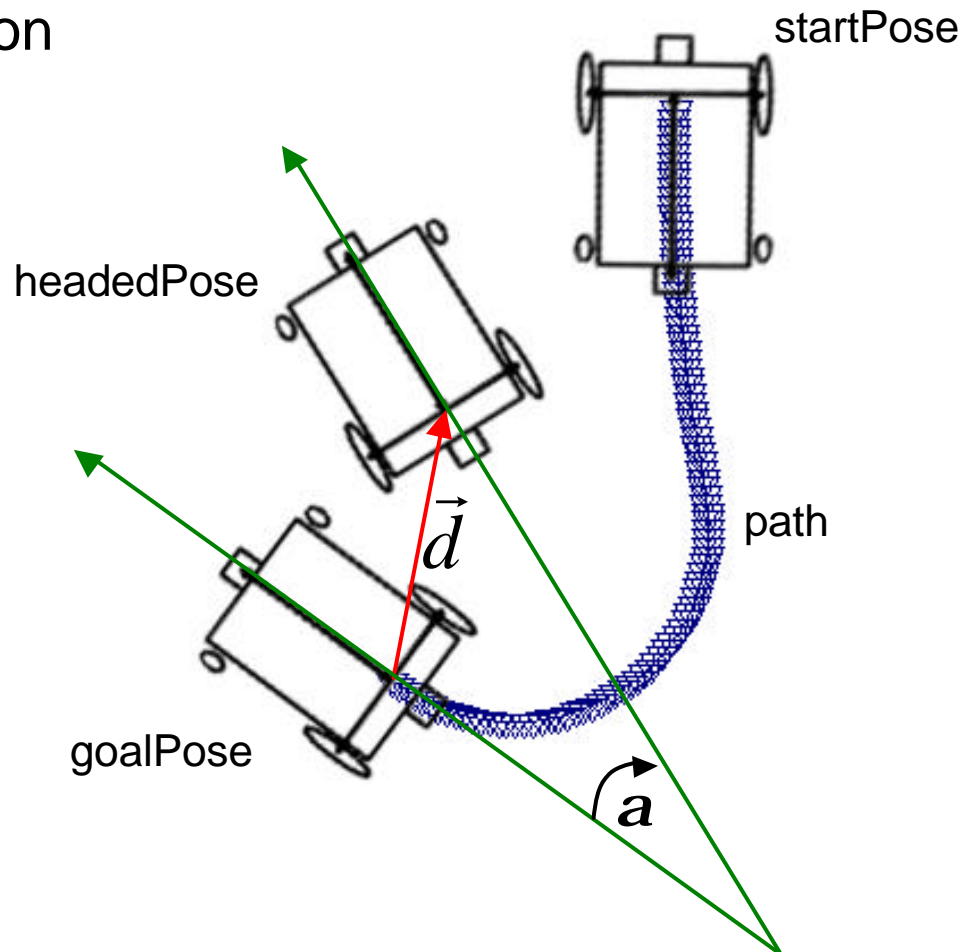


Test-for-Collision-Operation has to rotate CT-entries.



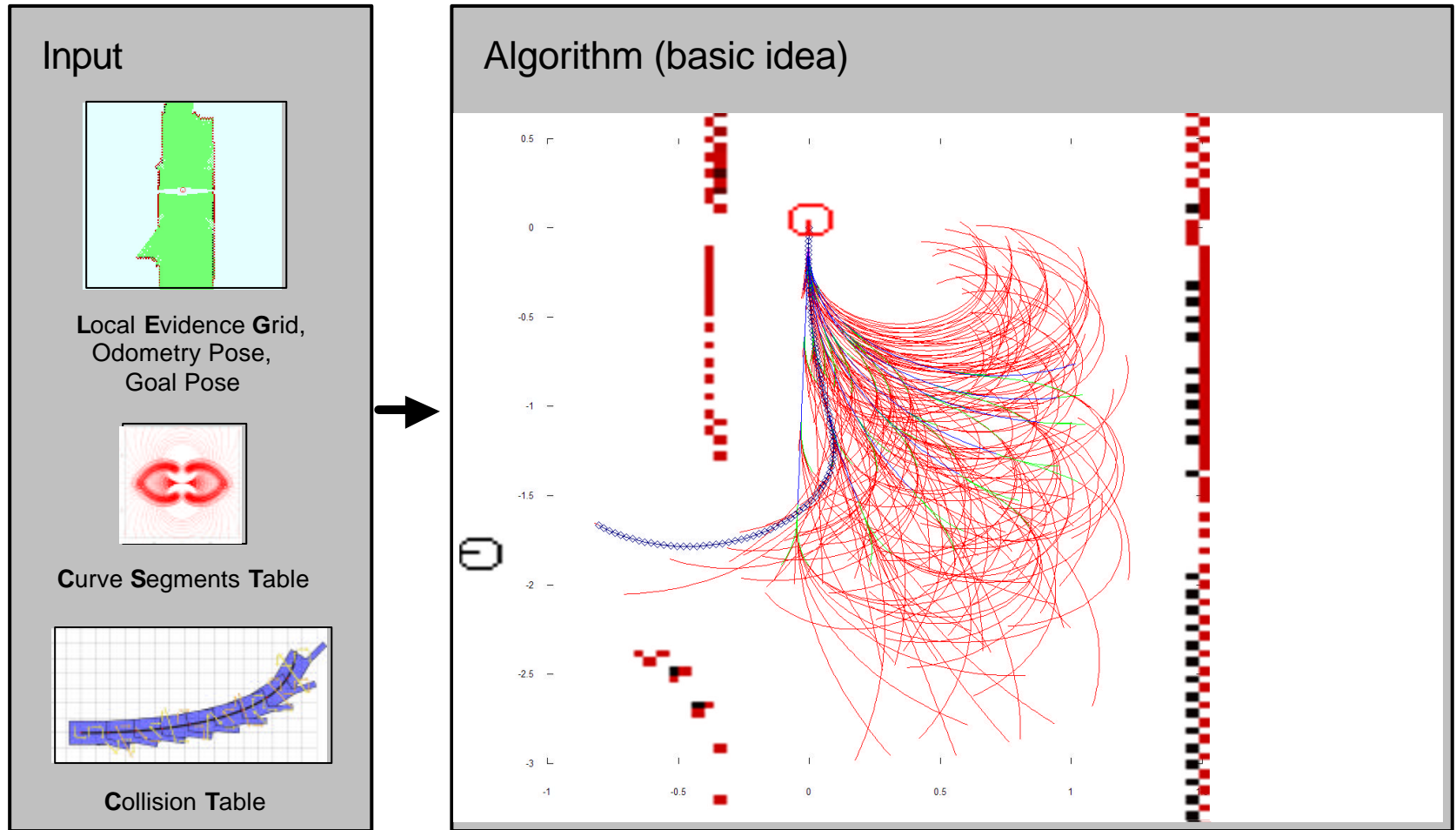
Precompute additional table which holds rotated
offsets between occupied cells.

Score Function



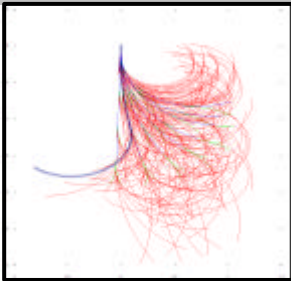
$$score(path, startPose, headedPose) = |\vec{d}| + c_1 * a + c_2 * path.length$$

Computing the Optimal Path



Algorithmic Refinements 2

Goal:
reduce complexity
of computation



Computing the
optimal path w.r.t.
objective function



Algorithm (with constant *arc2.length*)

set *arc2.length* = *MAX_arc2.length*

\forall *arc1.curvature*, *arc1.length*, *arc1.direction* do

\forall *arc2.curvature*, *arc2.direction* do

- construct *path*
- test for collision and prune if necessary
- minimise *path.score*
- if (*path.score* < *bestPath.score*)
set *bestPath* = *path*

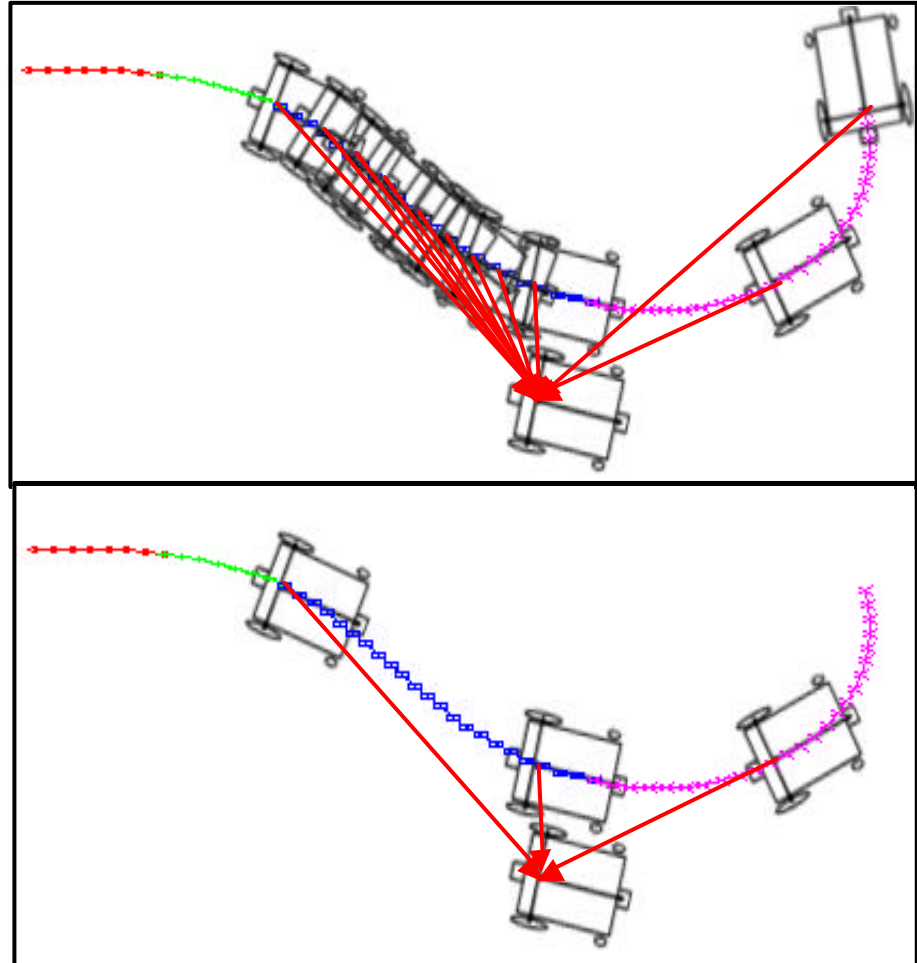
Algorithmic Refinements 3

Algorithm
(with constant
arc2.length)

minimise
path.score

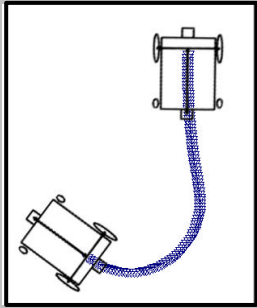
\forall potential *goalPose*
 \in *arc2* do

- *calc score*
- store *goalPose*
with minimal score



Computing the Velocity Profile

Input



Solution Path

$path = \{pose_0, \dots, pose_n\}$

Velocities in Start & Goal

v_{start}, v_{goal}

Lateral Acceleration Limit

a_{max}

Longitudinal Acceleration Limit

v_{max}

Rotational Velocity Limit

w_{max}

Longitudinal Velocity Limit

v_{max}

Algorithm

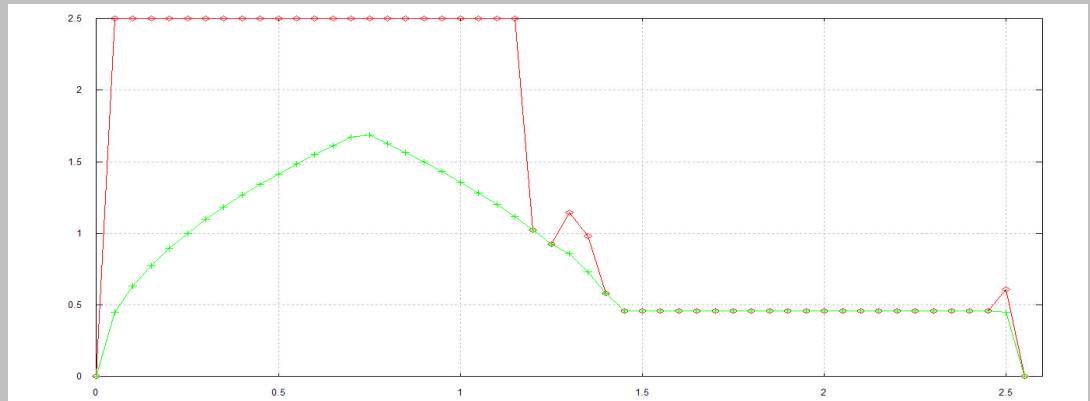
FOR EVERY $pose_i \in path$ DO:

COMPUTE MAXIMUM velocity v_i FOR WHICH HOLDS:

$$|v_i| = \min(v_{max}, \sqrt{\frac{a_{max}}{pose_i.c}}, \frac{w}{pose_i.c})$$

FOR EVERY v_i DO:

INCORPORATE LONGITUDINAL ACCELERATION LIMIT v'_i :



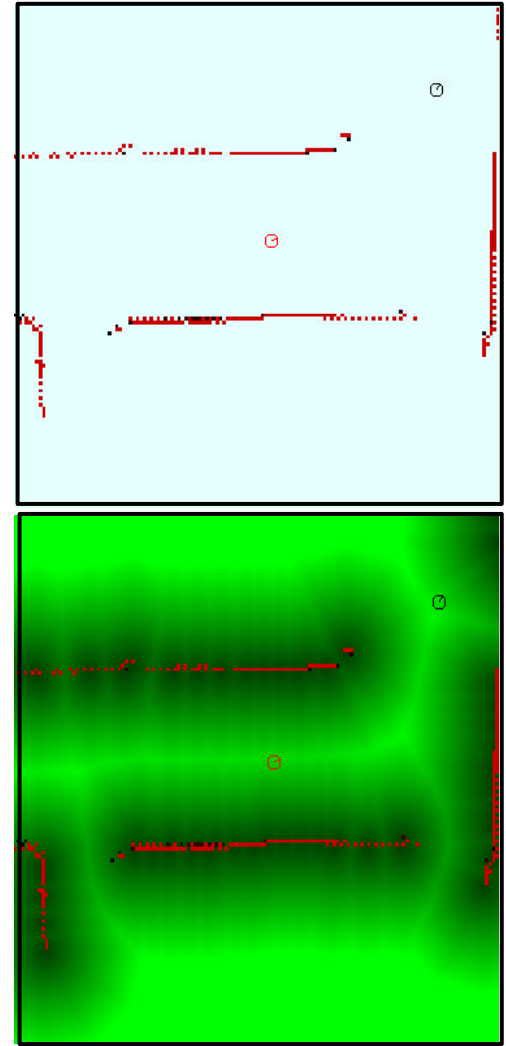
What remains to do

- current implementation considers only binary information from the evidence grid while doing the collision test
- better: collision test should also return minimal distance to obstacles for tested path



$score(path, startPose, headedPose) =$

$$|\vec{d}| + c_1 * \mathbf{a} + c_2 * path.length + c_3 * distToObstacles$$



Preliminary Experiments

